

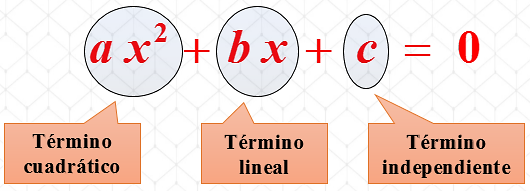
**Introducción al Cálculo -MA611**

**Semana N°2 Sesión 2**

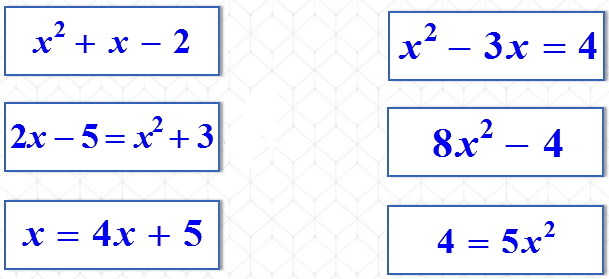
**Ecuaciones de cuadráticas o de segundo grado.**

Una ecuación cuadrática con una variable o también llamada ecuación de segundo grado, es toda ecuación que tiene la siguiente forma:

donde ***a***, ***b*** y ***c*** son parámetros (*a* **≠** 0), y ***x*** es la variable o incógnita.



**¿Cuáles son ecuaciones cuadráticas?**

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**Resolución usando la fórmula general**

Sea una ecuación cuadrática de la forma *ax*2 *+ bx + c =* 0*,* (*a, b, c números reales, con a ≠* 0)

Si la expresión *b*2 – 4*ac ≥* 0, entonces la solución en los **reales** de la ecuación está dada por:

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**Ejemplos:** Identifique los coeficientes en las ecuaciones mostradas y resuelva con ayuda de la calculadora:

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**Ejercicios:** Identifique los coeficientes en las ecuaciones mostradas y resuelva con ayuda de la calculadora:

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**Ejemplos:**

Determine el conjunto solución de cada una de las siguientes ecuaciones cuadráticas:

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**Ejemplo:**

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La utilidad mensual de una empresa**,** está dada por ***U* = −0,015 *x*2 + 12,34 *x* − 54,3** miles de dólares**,** para **"*x*"** cientos de unidades producidas y vendidas de cierto producto. Si la utilidad del mes anterior fue de 1 680 900 dólares, ¿cuántas unidades se han producido y vendido?

**Ejercicio:**

La utilidad mensual de una empresa, está dada por: *U* = −0,015*x*2 + 15,24*x* + 1 770,18 miles de dólares, para "*x*" cientos de unidades producidas y vendidas de cierto artículo. ¿Cuántas unidades se han producido y vendido en el mes donde la utilidad fue de 1 890 500 dólares?

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**Valor numérico de una expresión algebraica**

Es el número que adquiere la expresión algebraica al reemplazar las variables por números específicos.

**Ejemplo:** Calcule el valor numérico de *E* = 5*x*2 – 3*xy* + 7*y*3, para *x* = 3 e *y* = 2 .

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**Ejemplo:** En cierta familia, el gasto mensual en recreación es de “*G*” soles, el cual está relacionado con sus ingresos mensuales de “*x*” soles a través de la siguiente expresión:

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¿Cuánto gasta la familia en recreación cuando su ingreso mensual es de 2000 soles?

**Ejercicio 1:**

La cantidad de platos comida “*G*” que pueden preparar cierto grupo de cocineros de un restaurante está relacionado con el tiempo de “*x*” minutos que dedican ellos para elaborarlos a través de la siguiente expresión:



¿Cuántos platos habrán preparado los cocineros cuando la cantidad de tiempo que se dedicaron fue de 2 000 minutos?

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**Ejercicio 2: Interés Compuesto**

Para calcular el capital final (valor final) de un interés compuesto, capitalizable “*k*” veces al año, se utiliza la siguiente expresión:



Donde:

*P*: Capital.

*r*: Tasa de interés anual.

*t*: Tiempo en años y se capitaliza “*k*” veces al año.

Calcule el capital final que produce para: *P* = $ 1000 , *r* = 6% , *t* = 10 años y *k* = 12 .

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**Aplicaciones de las ecuaciones cuadráticas**

**Ejemplo:**

La Gerente administrativa de un restaurante sabe que, si mantiene el precio en 22 soles el kilo de comida, se venderán 1000 kilos al mes, pero el dueño tiene la idea de subir el precio para aumentar sus ingresos. Después de hacer un estudio de mercado se ha podido determinar que por cada sol que aumenta el precio se dejará de vender 20 kilos de comida al mes. Se hará una simulación para poder tomar decisiones sobre el precio en base a la siguiente tabla (complete la tabla):

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| **Aumento** | **Precio** | **Cantidad** | **Ingreso** |
| **0** | 22 | 1 000 | 22 000 |
| **1** |  | 1 000 – (1)(20) |  |
| **2** |  |  |  |
| **3** |  |  |  |
| **⁞** |  |  |  |
| ***x*** |  |  |  |

En base al problema propuesto y la tabla, responde los siguientes ítems:

1. Usando la tabla, represente con una expresión matemática el precio de un kilogramo de comida para cualquier aumento de “*x*” soles y la cantidad de kilogramos de comida para dicho aumento.

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1. ¿Cuántos kilos de comida se deben vender al mes para que el restaurante obtenga un ingreso igual a S/ 24 640?(Considerar el menor valor)

**Reflexión:**

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1. En la siguiente ecuación cuadrática  determina el valor .

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1. Dada *x*2 – 3*x* = 4, ¿se cumple que *a* = 1, *b* = 3 y *c* = 4?

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1. Determina el valor de , se cumple que x = 1 e y = 2?